at weight = Mis2( directPdf, brdfPdf at cosThetaOut = dot( N, L );

1 = E \* brdf \* (dot( N, R ) / pdf);

E \* ((weight \* cosThetaOut) / directPdf)
andom walk - done properly, closely follo

at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &

v = true;

ırvive;

## INFOMAGR – Advanced Graphics

Jacco Bikker - November 2022 - February 2023

## Lecture 14 - "TAA & ReSTIR"

 $(x,x')\left[\epsilon(x,x')+\int_{S}\rho(x,x',x'')I(x',x'')dx''\right]$ 

Welcome!



## Today's Agenda:

- Prerequisits
- Reprojection
- Resampling
- ReSTIR

```
O, N );
ref1 * E * diffuse;
= true;

MAXDEPTH)

survive = SurvivalProbability( diffuse a sestimation - doing it properly, closes aff;
radiance = SampleLight( &rand, I, &L, &llighters a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.z) > 0) &&
```



## Introduction

Towards Noise-free Path Tracing

Ingredients:

#### Convergence:

Average many samples, rely on the law of large numbers to approach E.

#### **Importance Sampling:**

"Work smarter, not harder", by taking better samples.

#### **Specialized techniques:**

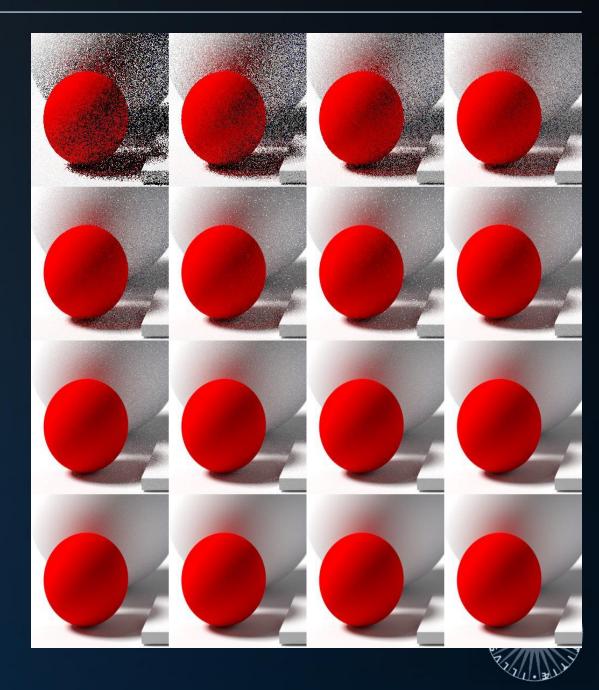
The right tool for the task; e.g. light tracing / photon mapping for caustics.



at weight = Mis2( directPdf, brdfPdf ); at cosThetaOut = dot( N, L ); E \* ((weight \* cosThetaOut) / directPdf)

n = E \* brdf \* (dot( N, R ) / pdf);

at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &



## Introduction

#### Towards Noise-free Path Tracing





Quake II RTX



E \* ((weight \* cosThetaOut) / directPdf) SEUS mod for Minecraft

vive)

at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf urvive; pdf; n = E \* brdf \* (dot( N, R ) / pdf);

## Introduction

**Towards Noise-free Path Tracing** 

#### Game graphics:

- 60fps
- 1spp
- ...
- Profit

#### But:

- It is good if it looks good
- Developer controls lights, geometry, camera (somewhat)

#### Opportunity:

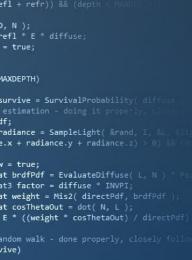
Trade some bias for performance.







The Tomorrow Children, PS4



at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &

1 = E \* brdf \* (dot( N, R ) / pdf);

## Today's Agenda:

- Prerequisits
- Reprojection
- Resampling
- ReSTIR

```
O, N );
ref1 * E * diffuse;
= true;

MAXDEPTH)

survive = SurvivalProbability( diffuse a sestimation - doing it properly, closes aff;
radiance = SampleLight( &rand, I, &L, &llighters a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.y + radiance.z) > 0) && (duffuse a sex + radiance.z) > 0) &&
```



```
at a = nt - nc,
(AXDEPTH)
survive = SurvivalProbability( diff)
radiance = SampleLight( &rand, I, &L, &
e.x + radiance.y + radiance.z) > 0) &&
v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * P
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf)
andom walk - done properly, closely followi
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &bd
ırvive;
pdf;
1 = E * brdf * (dot( N, R ) / pdf);
```

# ReSTIR, ingredient 1: Reprojection



Assumptions

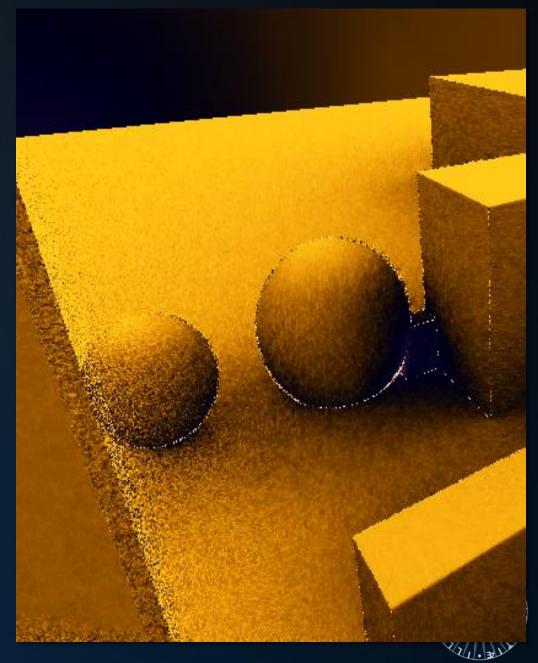
Converging requires a stationary camera.

Or: reprojection.

"where was pixel x,y in the previous frame?"

https://www.shadertoy.com/view/ldtGWl

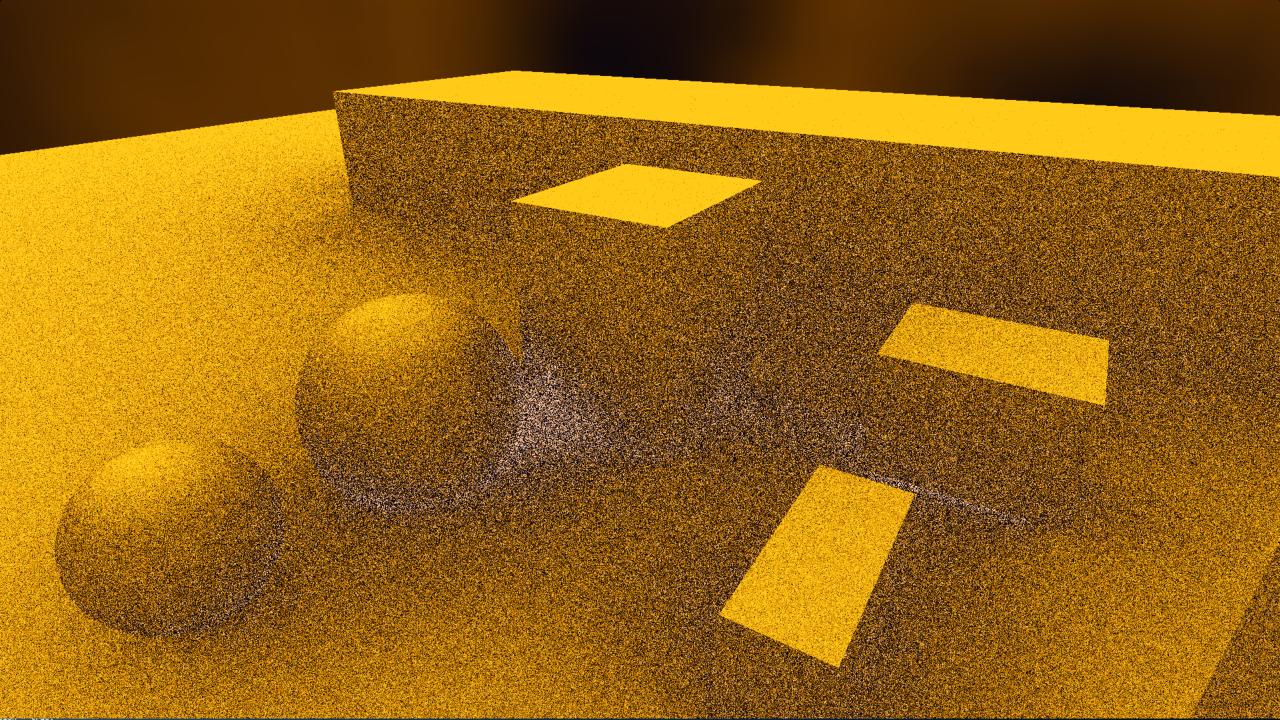


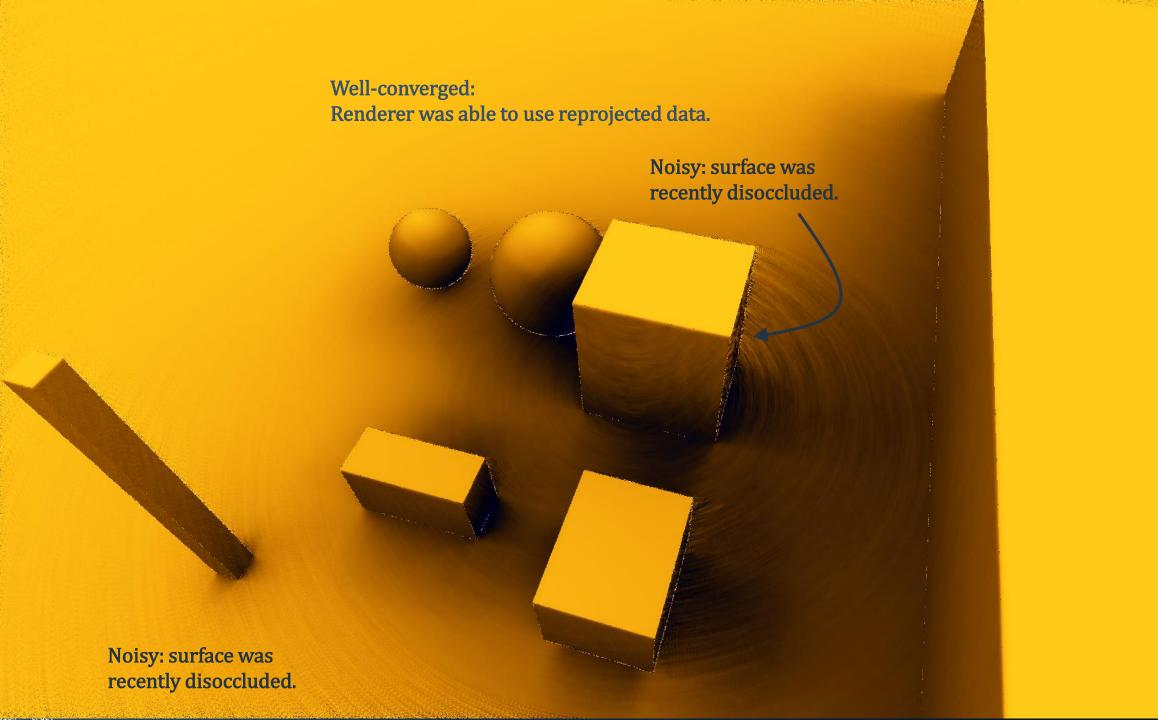


MAXDEPTH)

Survive = SurvivalProbability( diffuse estimation - doing it properly sites of the state of the st

1 = E \* brdf \* (dot( N, R ) / pdf);





**Practical Reprojection** 

Converging requires a stationary camera. Or: reprojection.

MPEG2 approach\*:

Using the color of pixel (x,y), search the neighborhood for a similar color. (problem: requires color of pixel (x,y), which (for path tracing) is noisy in the current and the previous frames).

Alternative, using additional data: using the world space position of the primary intersection point, search the neighborhood for the same position.

(we need to store a worldspace position per pixel) (we may need to store a worldspace positions per sample)







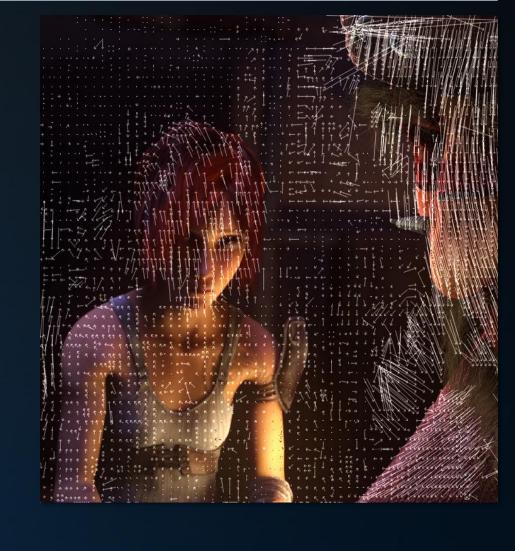
**Practical Reprojection** 

Rasterization approach\*:

In the vertex shader, transform the vertex with two matrices:

- 1. The current model/view/projection matrix;
- 2. The MVP matrix of the previous frame.

The difference is a (linear) *motion vector* per vertex. These are then interpolated over the triangle, yielding a motion vector per pixel.







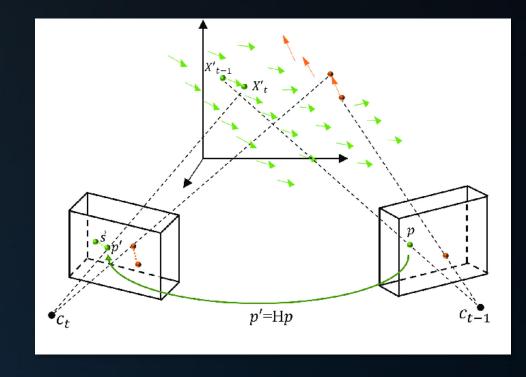


**Practical Reprojection** 

Poor man's approach:

Assume a fully static scene. Then:

- 1. Multiply the camera space primary intersection position by the inverse camera matrix;
- 2. Multiply the result by the camera matrix of the previous frame.

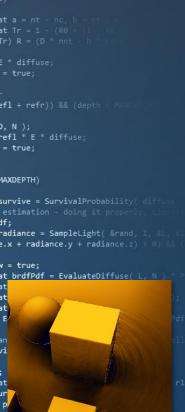


Or:

Use the planes of the view pyramid to determine where pixel (x,y) would have been in the previous frame.

(this method is implemented in Lighthouse 2).





#### Challenges

Sample convergence over many frames:

Keep a running average\*:

$$f_n(p) = \alpha \cdot s_n(p) + (1 - \alpha) \cdot f_{n-1}(\pi(p))$$

where



is the blending factor ( $\sim 0.1$ ),

 $\overline{s_n(p)}$  is frame n's new sample color at pixel p,

 $f_{n-1}(\pi(p))$  is the reprojected history color from the previous frame.





efl + refr)) && (depth

refl \* E \* diffuse;

), N );

at3 brdf = SampleDiffuse( diffuse, N, r1, 1 = E \* brdf \* (dot( N, R ) / pdf);

at weight = Mis2( directPdf, brdfPdf at cosThetaOut = dot( N, L );

E \* ((weight \* cosThetaOut) / directPdf andom walk - done properly, closely foll

#### Challenges

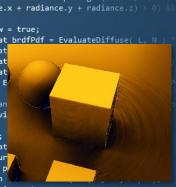
Reprojection may fail in several cases:

- 1. In the previous frame, pixel (x,y) was off-screen.
- 2. In the previous frame, pixel (x,y) was occluded.
- 3. Pixel (x,y) is on a specular surface, which is a view-dependent BRDF.
- 4. Pixel (x,y) was in the shadow of a moving light in the previous frame, now it isn't.
- 5. ...

#### Solutions:

Pragmatic. Case 1: drop the sample, we can't average with it. All other cases: clip\*.





refl \* E \* diffuse;



Advanced Graphics – ReSTIR

## Reprojection

#### **Further Reading**

#### THE CODE CORSAIR

AHOY WORLD!







SEARCH

POSTS

https://www.elopezr.com/temporal-aa-and-the-quest-for-the-holy-trail

#### TEMPORAL AA AND THE OUEST FOR THE HOLY TRAIL

BY ADMIN JANUARY 2, 2022 GRAPHICS

Long gone are the times where Temporal AA was a novel technique, and slowly more articles appear covering motivations, implementations and solutions. I will throw my programming hat into the ring to walk through it, almost like a tutorial, for the future me and for anyone interested. I am using Matt Pettineo's MSAAFilter demo to show the different stages. The contents come mostly from the invaluable work of many talented developers, and a little from my own experience. I will introduce a couple of tricks I have come across that I haven't seen in papers or presentations.

#### Sources of aliasing

The origin of aliasing in CG images varies wildly. Geometric (edge) aliasing, alpha testing, specular highlights, high frequency normals, parallax mapping, low resolution effects (SSAO, SSR), dithering and noise all conspire to destroy our visuals. Some solutions, like hardware MSAA and screen space edge detection techniques, work for a subset of cases but fail in different ways. Temporal techniques attempt to achieve supersampling by distributing the computations across multiple frames, while addressing all forms of aliasing. This stabilizes the image but also creates some challenging artifacts.

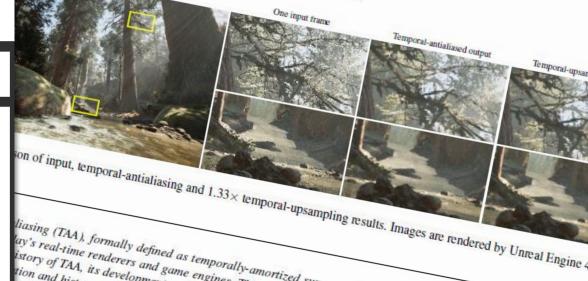
#### **Jitter**

The main principle of TAA is to compute multiple sub-pixel samples across frames, then combine those together into a single final pixel. The simplest scheme generates random samples within the pixel, but there are better ways of producing fixed sequences of samples. A short overview of quasi-random sequences can be found here. It is important to select a good coguence to avoid dumning and a discrete number of camples within the coguences twically between 4.0 we

# A Survey of Temporal Antialiasing Techniques

Lei Yang, Shiqiu Liu, Marco Salvi

NVIDIA Corporation



Temporal AA and the guest for the Holy Trail January 2, 2022

The Rendering of Mafia: Definitive Edition August 23, 2021

A Macro View of Nanite May 30,

The Rendering of Jurassic World: Evolution March 12, 2021

Rendering Line Lights July 10, 2019

The Rendering of Rise of the Tomb Raider December 31, 2018 A real life pinhole camera January 14, 2018

The Rendering of Middle Earth: Shadow of Mordor December 27

liasing (TAA), formally defined as temporally-amortized supersampling, is the most widely used antialiasing assing (1AA), Jormany aginea as temporatry-amortized supersampting, is the most widely used annualising and the state of TAA its devaluation and related word. We then identify the free main enh-components of TAA. istory of TAA, its development path and related work. We then identify the two main sub-components of TAA,

is and discourse allowithmic and involuntation options. As townward involuntation in the sub-components of TAA, tion and history validation, and discuss algorithmic and implementation options. As temporal upsampling is ingly relevant to today's game engines, we propose an extension of our TAA formulation to cover and to some the cover and to some the cover and the cover an pling techniques. Despite the popularity of TAA, there are still significant amounts.



## Today's Agenda:

- Prerequisits
- Reprojection
- Resampling
- ReSTIR

```
p, N );
refl * E * diffuse;
= true;

MAXDEPTH)

survive = SurvivalProbability( diffuse not estimation - doing it properly, close of the state o
```



```
efl + refr)) && (depth < MA
(AXDEPTH)
survive = SurvivalProbability( diff)
radiance = SampleLight( &rand, I, &L, &
e.x + radiance.y + radiance.z) > 0) &&
v = true;
at brdfPdf = EvaluateDiffuse( L, N ) * F
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf)
andom walk - done properly, closely followi
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &bd
ırvive;
pdf;
1 = E * brdf * (dot( N, R ) / pdf);
```

# ReSTIR, ingredient 2: Resampling



Importance Sampling Lights

Sampling *N* lights with *1* ray:

Use a constant discrete pdf:  $\rho_i = \frac{1}{N}$ , where  $i \in [1..N]$ .

0r:

Use importance sampling.

But, what is the importance of each light? We can use the *potential contribution\** of each light:

$$L_p = E \frac{A \cos \theta_i \cos \theta_o}{d^2}$$

#### Note:

- We calculate the potential contribution for each light, at each path vertex.
- We create a discrete *cdf* over the lights (CDF: cumulative distribution function).
- To pick one light, we need to walk the cdf a second time.



N = 10:

{ 1/42, 3/42, 6/42, ... }

That is: the emittance of the light, scaled by its solid angle, as seen from a point in the scene.



\*: Note: the potential contribution may differ significantly from the actual contribution!

1 = E \* brdf \* (dot( N, R ) / pdf);

at weight = Mis2( directPdf, brdfPdf

andom walk - done properly, closely f

at3 brdf = SampleDiffuse( diffuse, N, r1

efl + refr)) && (dept

refl \* E \* diffuse;

```
radiance = SampleLight( &ran
e.x + radiance.y + radiance
at brdfPdf = EvaluateDiffuse
at3 factor = diffuse * INVPI
at weight = Mis2( directPdf
at cosThetaOut = dot( N, L
E * ((weight * cosThetaOut)
```

at3 brdf = SampleDiffuse( diffuse, N, r1, r2, & urvive; pdf; n = E \* brdf \* (dot( N, R ) / pdf);

(AXDEPTH)

v = true;

From Multiple to *Many* Lights

Challenge:

Picking a light with a probability proportional to its potential contribution requires evaluation of all lights, i.e.:

- Fetching light properties from memory;
- Calculations: includes  $1/r^2$ ,  $\cos \theta$ , BRDF evaluation;
- Storing the result in the cdf array.

If we have more than a dozen or so lights, this is not feasible.

Solution: *precalculate potential* contribution?

```
(AXDEPTH)
radiance = SampleLight( &rand,
at weight = Mis2( directPdf, brdfPdf
```

andom walk - done properly, closely fo

n = E \* brdf \* (dot( N, R ) / pdf);

at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R.

), N );

From Multiple to *Many* Lights

Potential contribution is proportional to:

- Solid angle
- Brightness of the light

Sadly, we cannot pre-calculate potential contribution; it depends on the location and orientation of the light source relative to the point we are shading.

We can however precalculate a less refined potential contribution based on:

- Area
- Brightness

```
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf) * (radion
andom walk - done properly, closely following sand
vive)

;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &
urvive;
pdf;
i = E * brdf * (dot( N, R ) / pdf);
sion = true:
```

), N );

(AXDEPTH)

v = true;

refl \* E \* diffuse;

survive = SurvivalProbability( diff

radiance = SampleLight( &rand, I, & e.x + radiance.y + radiance.z) > 0)

at brdfPdf = EvaluateDiffuse( L, N

Many Lights Array

0|1|2|... ...|M-1

The light array stores pointers to (or indices of) the lights in the scene. For *N* lights, light array size *M* is several times *N*.

Each light occupies several consecutive slots in the light array, proportional to its (coarse) potential contribution.

Selecting a random slot in the light array now yields (in constant time) a single light source L, with a probability of  $\frac{slots\ for\ L}{M}$ .



E \* ((weight \* cosThetaOut) / directPdf) \* (radius)
andom walk - done properly, closely following second
vive)
;
st3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf
urvive;
pdf;
n = E \* brdf \* (dot( N, R ) / pdf);
sion = true:

), N );

(AXDEPTH)

refl \* E \* diffuse;

survive = SurvivalProbability( dif

radiance = SampleLight( &rand, I

at weight = Mis2( directPdf, brdfPdf at cosThetaOut = dot( N, L );

Resampled Importance Sampling\*

0|1|2|... ...|M-1

The light array allows us to pick a light source proportional to importance. However, this importance is not very accurate.

We can improve our choice using *resampled importance sampling*.

- 1. Pick *N* lights from the light array (where *N* is a small number, e.g. 4);
- 2. For each of these lights, determine the more accurate potential contribution;
- 3. Translate the potential contribution to importance (using a small cdf);
- 4. Choose a light with a probability proportional to this importance.

This scheme allows for unbiased, accurate and constant time selection of a good light source.

st3 brdf = SampleDiffuse( diffuse, N, r1, r2,\*: Importance Resampling for Global Illumination, Talbot et al., 2005.

pdf; n = E \* brdf \* (dot( N, R ) / pdf); sion = true:

at weight = Mis2( directPdf, brdfPdf

andom walk - done properly, closely t

efl + refr)) && (dep

refl \* E \* diffuse;

```
(AXDEPTH)
survive = SurvivalProbability( diff)
radiance = SampleLight( &rand, I, &L,
e.x + radiance.y + radiance.z) > 0) 88
v = true;
at brdfPdf = EvaluateDiffuse( L, N )
at3 factor = diffuse * INVPI;
at weight = Mis2( directPdf, brdfPdf );
at cosThetaOut = dot( N, L );
E * ((weight * cosThetaOut) / directPdf)
/ive)
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &
ırvive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
```

https://www.youtube.com/watch?v=Znr1JJLI5uY



## Today's Agenda:

- Prerequisits
- Reprojection
- Resampling
- ReSTIR

```
p, N );
refl * E * diffuse;
= true;

MAXDEPTH)

survive = SurvivalProbability( diffuse not estimation - doing it properly, close of the state o
```



```
cics
k (depth < MAXDEFIE)

c = inside ? I = I = I

tt = nt / nc, ddn = I = I

so ta = nt - nc, b = nt = re

at Tr = 1 - (R0 + (1 - R0

Tr) R = (D * nnt - N * (ddn

E * diffuse;
= true;

cefl + refr)) && (depth < MAXDEFIE)

AXXDEPTH)

survive = SurvivalProbability( diffuse;
estimation - doing it properly, classif;
radiance = SampleLight( &rand, I, &L

ext + radiance.y + radiance.z) > 0)
```

ReSTIR\*

Ingredient 1:

Reprojection

**Ingredient 2:** 

Resampling.

Ingredient 3:

Streaming RIS.







et brdfPdf = EvaluateDiffuse( L, N ) \* at3 factor = diffuse \* INVPI; at weight = Mis2( directPdf, brdfPdf ) at cosThetaOut = dot( N, L );

E \* ((weight \* cosThetaOut) / directPdf)

ReSTIR\* - Direct Light from a Very Large Number of Lights

Algorithm, in short:

Sample millions of lights for a pixel with one ray to an important light.

To pick the important light:

- 1. Use RIS;
- 2. Consider the knowledge of the neighbors;
- 3. Consider the knowledge of the past.

Hence: spatio-temporal resampling.

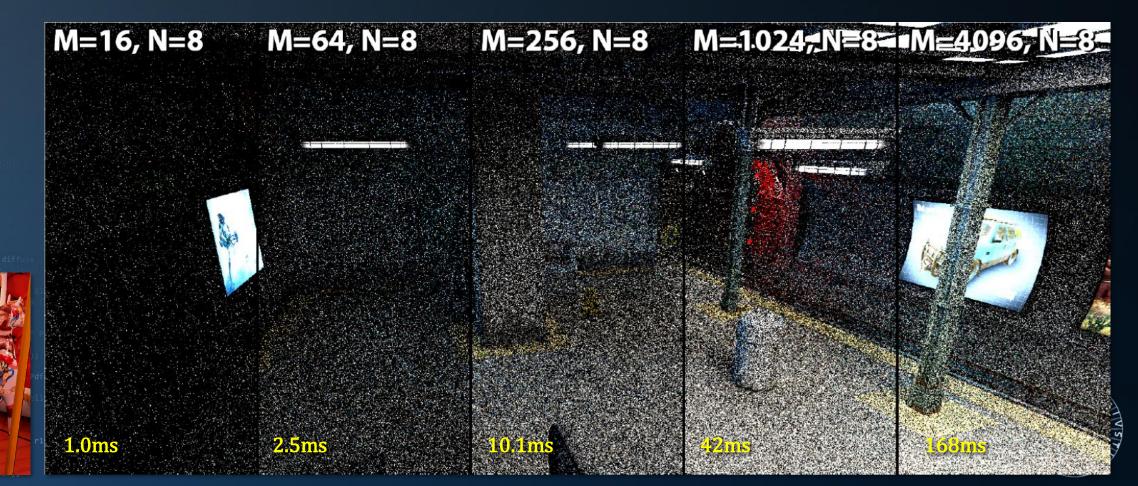


<sup>\*:</sup> Spatiotemporal reservoir resampling for real-time ray tracing with dynamic direct lighting, Bitterli et al., 2020.



ReSTIR\* - Direct Light from a Very Large Number of Lights

Applying RIS:



Weighted Reservoir Sampling

Recall:

Selecting a light with a probability proportional to its potential contribution:

- 1. Calculate and store the weight of each light
- 2. Calculate the sum *S* of the weights
- 3. Draw a random number in the range [0...S)
- 4. Walk the array of stored weights until the running sum exceeds S.

#### Problems:

- Storage;
- Visiting the data twice.





Weighted Reservoir Sampling

Alternative approach:

```
y = 0, w_{sum} = 0

for each light index i with weight w_i

w_{sum} += w_i

if (rand() < w_i / w_{sum}) y = i;
```

After processing all lights, y contains the chosen light.

- No storage
- Data is visited only once

There is a third, somewhat hidden benefit:

After choosing the light, we still have the reservoir state in y and  $w_{sum}$ .





#### Back to ReSTIR

Combining the ingredients:

1. Pass 1: for each pixel, use reservoir sampling to pick a light.

Result: a reservoir state, consisting of light index y, and  $w_{sum}$ .

2. Pass 2: for each pixel, combine reservoirs of neighborhood.

Result: neighborhood combines forces to pick much better lights.

3. And finally: store final reservoirs for the next frame.

Result: good picks of previous frames become candidates in the current frame.

The light to which we finally send a shadow ray to is effectively taken from a massive pool of candidates.





ReSTIR\* - Direct Light from a Very Large Number of Lights

Neighbors & the past:









## Today's Agenda:

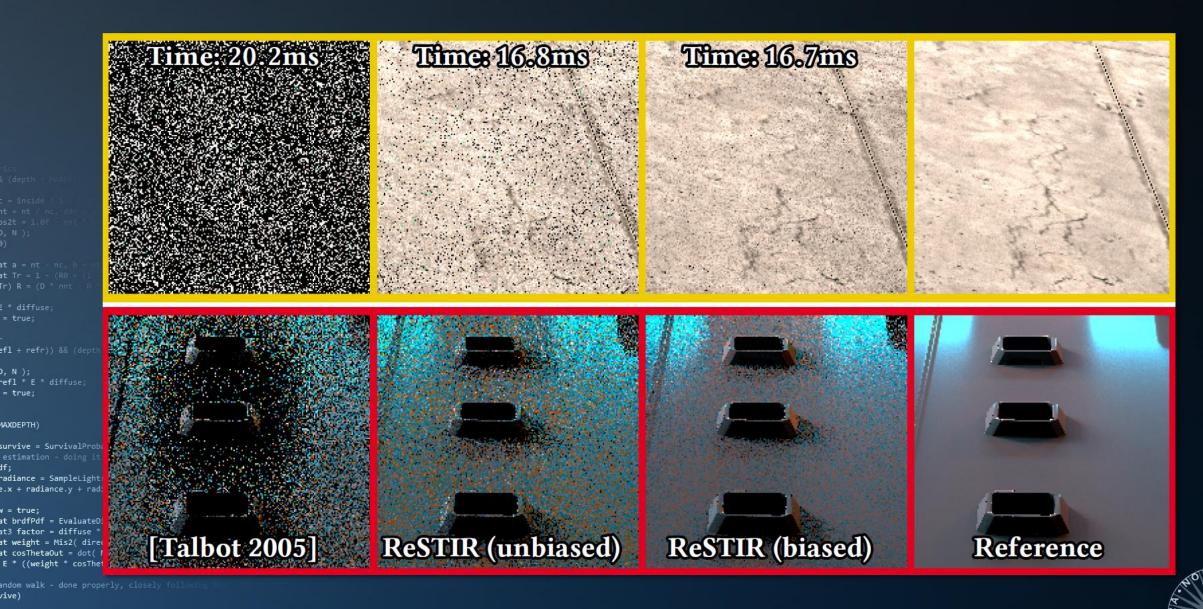
- Prerequisits
- Reprojection
- Resampling
- ReSTIR

```
p, N );
refl * E * diffuse;
= true;

MAXDEPTH)

survive = SurvivalProbability( diffuse not estimation - doing it properly, close of the state o
```





There's still noise... now what?

at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, & 1 = E \* brdf \* (dot( N, R ) / pdf);

(AXDEPTH)

## INFOMAGR – Advanced Graphics

Jacco Bikker - November 2022 - February 2023

## END of "ReSTIR"

next lecture: "Filtering & Learning GI"



efl + refr)) && (depth < MA

refl \* E \* diffuse;

), N );

